

山地流域における降雨量の変化

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Variation in Storm Rainfall over Mountainous Basin

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We deal here with the problem how variation in average storm rainfall over mountainous basin is caused by the number of rain-gages installed in those area. Two methods—Thiessen polygon method and isohyetal method—are compared as regard to computation of average rainfall. Also examined is the relation between the point rainfall and areal-average rainfall over a drainage basin which varies with the size of the governing area when a single rain-gage is located in the basin. In these cases a single storm is taken as a unit of rainfall.

The total runoff is computed for each single storm, and the relation between areal-average rainfall and total runoff is taken into account.

Introduction

In order to obtain "precise data" on precipitation and discharge, we have chosen the greater part of the Kanna River basin (one of the upper tributaries of the Tone River shown in Fig. 1) as experimental basin and started field observations in 1948. While the first three years were spent in arranging various measuring instruments and in training of observers, and since 1951 we have been getting pretty accurate data.

In our experimental basin 30 rain-gages are located as shown in Fig. 2. For the convenience of observation, three types of self-recording rain-gages are used separately as follows: one day rain-gages along the main stream, a fortnight rain-gages in the basins along the main tributaries, and "Sugaya" rain-gages* all around the basin.

Elevation and type of each rain-gage are indicated in Table 1.

We have a gaging station at the lowest end of the experimental basin. At this station discharge is measured twice a day usually and many times during flood time.

Features of the basin

Fig. 3 shows that proportion of the length of the stream to the size of the basin is approximately definite, as it would be guessed from the shape of the basin. The profile of the main stream is shown in Fig. 4: total length is 66 kilometers, the elevation of the headwaters 1974 meters and that of the gaging station 130 meters. The Kanna River flows into the Karasu

River (a branch of the Tone River) at a point 15 kilometers below the station.

The river bed maintains nearly uniform slope of $\frac{1}{110}$ for about 50 kilometers above the station.

The area-elevation curve of the experimental basin is shown in Fig. 5.

Basic data

Rainfall may be differently determined according to the length of time of observation. And we use in this paper a single storm as the basis of study. Table 2 indicates 42 cases (with rainfall over 10 millimeters) which are selected out of the data obtained from 1951 to 1953.

Average rainfall calculated by Thiessen polygon method

Each of the Figs. 6 (1), (2), (3), (4) and (5) shows Thiessen polygon for 30, 16, 8, 4 or 2 stations respectively in the whole basin. In each case every station has its governing area shown in Table 3. Gages had been so located that they may have governing areas of approximately same size, but some fluctuation occurred especially along the border-line of the basin: (the average of area being calculated by dividing total basin area by the number of station installed in it). Then differences between the average rainfall for 16, 8, 4 and 2 stations and the average rainfall for 30 stations respectively for each storm should be computed. The error is defined as the difference divided by the average rainfall for 30

* A galvanized recording rod is dipped in the solution of sulphuric acid. Each single storm is marked on the surface of recording rod as a bite.

stations for each of 29 storms. Fig. 7 shows the relation between the average governing area and the error for these storms.

Average rainfall calculated by isohyetal method

30, 16, 8 and 4 stations are selected as are in the case of the Thiessen polygon method. Isohyetal lines are drawn for 30, 16, 8 and 4 stations and average rainfall is computed from each map. Fig. 8 (1), (2), (3) and (4) show the isohyetal maps for 30, 16, 8 and 4 stations in the case of No. 12 storm. The error means the difference divided by the average rainfall for 30 stations for each of 29 storms as it is in the Thiessen polygon method. The relation between the governing area and the error for each storm are shown in Fig. 9.

Comparing the average rainfall computed by both the Thiessen polygon method and the isohyetal method at 30 stations, we found no greater difference than 4.5 % for 30 storms.

The envelopes for points in Fig. 7 and 9 are shown in Fig. 11. These two envelopes are very close each other and symmetry about the horizontal axis.

Representativeness of point rainfall method

While the amount of rainfall over a drainage basin is computed by means of several rain-gages located on the basin, it may be sometimes determined, if necessary, by means of a single rain-gage directly. The foregoing two cases correspond to the former, and the present case falls to the latter.

The original basin is subdivided as illustrated by Fig. 10. For respective subdivisions the average rainfall is computed by isohyetal maps for 24 storms. In each subdivision a representative station is decided on condition that the station has sufficient data, the station lies near the center of it and the variance on the station is small. Fig. 12 shows the relation between the governing area by a single rain-gage and the error for each storm. In this case an envelope cannot be drawn, but we find the smaller is an area, the less variance exists.

Normal recession curve

Out of the numerous time-discharge curves obtained by our measuring station from 1948 to 1953, 45 recession curves for dry days are picked up. A normal recession curve as shown in Fig. 13 is obtained, by drawing these curves of the same scale for all the cases and overlapping the same portion of time-discharge curves starting from the smallest discharge. This diagram shows that features for each rain remains for a certain period then they vanish gradually until every curve coincides with a single curve named normal recession curve. The initial part of this curve is considered affected by inter flow as well as by ground water flow, but the final one by ground water flow only.

The limit of application of this curve is as follows :

maximum discharge is 80 cubic meters per second, minimum discharge 2.5 cubic meters per second and duration about 60 days.

This curve is plotted on a semi-log paper and the final part of this curve is considered as a straight line, while the initial one cannot be considered so though as a whole it may be said so.

Computation of runoff

It is assumed that the time-discharge curve ABCDEF shown in Fig. 14 (1) is already obtained. If the curve AB coincides with the normal recession curve, it would continue to trace the extension of the normal recession curve BG (G lies at the infinity), supposed there is no rain after B. Total runoff due to the precipitation after B may be represented by the area GBCDEF. Also assumed is that the curve CDEF coincides with the normal recession curve after D. Drawing a line parallel to the abscissa from the point B (BI means "discharge at beginning of rise") the point E is obtained on the curve DF. It is obvious that $BI = EJ$. The curve BG and curve EF are parallel because they both are a portion of the normal recession curve and the starting points are of the same value. Accordingly it is evident that $GBEF = IBEJ$. Therefore, the total runoff $GBCDEF = IBCDEJ$. The total runoff caused by a single storm is to be computed by summing up the discharge over a period from the beginning of rise to the time corresponding to a point of the same ordinate on the falling discharge hydrograph.

When the falling curve due to the first precipitation is too near the next rising curve due to the second precipitation as shown in Fig. 14 (2), the point corresponding to E in the former diagram cannot be observed. If a portion of curve CDK coincides with the normal recession curve, the curve DK should be extended along the normal recession curve and the point E corresponding to the point B should be obtained on the curve KF. The total runoff caused by a single storm in this case is obtained by the same way mentioned above.

There may be some cases when curve AB or CD does not coincide with the normal recession curve exactly. Two cases are shown in Fig. 14 (3) and (4) . In such cases the total runoff is computed by assuming that point B or D passes through the normal recession curve. Then, the accurate value is estimated as more or less than the computed value by giving a symbol \uparrow and \downarrow to each case.

Runoff and Runoff Coefficient

Table 4 indicates the average rainfall, runoff, runoff coefficient and discharge at beginning of rise for 28 cases. From these values the relation between the average rainfall and runoff using discharge at beginning of rise as a parameter is shown in Fig. 15. When the discharge at beginning of rise increases, the

straight line passing through the origin and inclining at 45 degrees to the abscissa should be a asymptote for these points. The same relation is observed between the average rainfall and runoff coefficient using the discharge at beginning of rise as a parameter. (Fig. 16)

Summary

It should be emphasized that this study is based on the limited data obtained from for a single locality. We can use either the Thiessen polygon method and the isohyetal method for the computation of average rainfall, if a rain-gage is located in every 12 square kilometers and error of 5 % is permitted.

There is little difference between Fig. 7 and 9

showing the relation between the governing area of stations and the error. If error is not permitted to be more than 10 %, a rain-gage should be located for every 25—30 square kilometers.

If a single rain-gage is located in a certain basin, the variance for the station becomes smaller by narrowing its governing area as shown in Fig. 12.

In Fig. 15 and 16 we are unable to get separate curves using the discharge at begining of rise as a parameter. It may be due partly to difficulty of field observation, and partly to an inadequate method of computation of runoff. At any rate it may be said that there is a certain relation between them.

Table 1. Elevation and type of rain-gages

Rain-gage No.	Elevation (m)	Type
01	980	Self-recording, for one day
02	700	Self-recording, for one day
03	540	Self-recording, for one day
04	600	Self-recording, for one day
05	700	Self-recording, for one day
06	820	Self-recording, for one day
07	340	Self-recording, for one day
08	250	Self-recording, for one day
09	130	Self-recording, for one day
11	800	Self-recording, for two weeks
12	900	Self-recording, for two weeks
13	720	Self-recording, for two weeks
14	450	Self-recording, for two weeks
21	1828	Sugaya
22	1549	Sugaya
23	1700	Sugaya
24	1580	Sugaya
25	1280	Sugaya
26	1060	Sugaya
27	1460	Sugaya
28	1220	Sugaya
29	900	Sugaya
30	780	Sugaya
31	1420	Sugaya
32	970	Sugaya
33	770	Sugaya
34	716	Sugaya
35	700	Sugaya
36	650	Sugaya
41	370	Non self-recording

Table 2. (2) Data of Storm Precipitation

Storm Precipitation	Rain-gage No.		Period						
	12	03	13	27	04	28	05		
1	June	15-16, 1951		54					
2	July	2, 1951		91				87	
3	July	4-5, 1951		20				36	
4	July	8-9, 1951		6					
5	July	10-11, 1951		66					
6	September	24-27, 1951		37				48	
7	September	29-30, 1951		1					
8	October	13-15, 1951		33				60	
9	May	22-28, 1952	14	14	13	21	10	15	14
10	June	2, 1952	15	13	19	14	13	21	18
11	June	8-10, 1952	24	18	26	24	16	30	23
12	June	22-25, 1952	82	81	87	94	80	90	77
13	July	2-3, 1952	26	26			33	27	28
14	July	3-4, 1952	15	25			10	31	22
15	July	4, 1952	21	22	8	18	14	25	25
16	July	9-12, 1952	44	38	40	46	46	52	43
17	July	13-15, 1952	32	42	40	33	43	42	40
18	July	17-20, 1952	27	19	17	49	26	29	19
19	August	7-8, 1952	49	25	40	60	33	30	27
20	August	31, 1952	25	13	14	12	15	16	13
21	September	6-10, 1952	34	30	25	34	24	51	31
22	September	11-16, 1952	25	26	26	20	17	25	26
23	October	6-8, 1952	20	21	18	29	28	30	28
24	October	27-28, 1952	22	19	18		16	23	19
25	November	4-5, 1952	28	30	34		32	31	
26	May	5-6, 1953		9				7	10
27	May	7-9, 1953		22	32	27	23	33	24
28	May	23-24, 1953	55	47	50	44	47	56	49
29	June	6-8, 1953	66	54	45		48	53	
30	June	10-12, 1953	17	17	18		18	21	
31	July	3-4, 1953	61	58	57		54	60	
32	July	7-8, 1953	20	13	18		14	16	
33	July	9-11, 1953	31	26	30		27	37	
34	July	16-19, 1953	34	33	35		35	33	30
35	July	20, 1953	59	75	77		76	73	
36	July	20-23, 1953	49	45	42		40	42	
37	September	23-25, 1953	109	100	107	107	117	120	116
38	September	29-30, 1953	18	10	7		7	15	12
39	October	2, 1953	28	32	47	54	51	36	36
40	October	9, 1953	19	14	17	14	16	21	14
41	October	28, 1953	6	8	6	9	9	11	8
42	October	28-30, 1953	8	18	11	36	21	15	23

Table 2. (1) Data of Storm Precipitation

Table with columns: Storm Precipitation, Period, Rain-gage No., 21, 22, 01, 23, 24, 11, 02, 25, 26. Rows include dates from June 1 to October 42, 1951-1953.

Table 2. (3) Data of Storm Precipitation

Table with columns: Storm Precipitation, Period, Rain-gage No., 29, 14, 30, 41, 31, 32, 06. Rows include dates from June 1 to October 42, 1951-1953.

Table 2. (4) Data of Storm Precipitation

Table with columns: Storm Precipitation, Period, Rain-gage No., 07, 33, 08, 34, 35, 36, 09. Rows include dates from June 1 to October 42, 1951-1953.

Table 3. Governing Area of Rain-Gate determined by Thiessen Polygon Method.

Table with columns: Number of Rain-gage, Average Governing Area (km²), Rain-gage No., 30, 16, 8, 4, 2. Rows list rain-gage numbers and their corresponding governing areas.

Table 4. Average Storm, precipitation, runoff, runoff coefficient and discharge at beginning of rise.

Storm Precipitation	Period	Average Storm Precipitation (mm)	Runoff (mm)	Runoff Coefficient (%)	Discharge at beginning of rise (3 m ³ /sec)
1	June 15-16, 1951	58.5	29.7	50.8	3.2
2	July 2, 1951	77.4	104.7	98.8	4.3
3	July 4-5, 1951	27.3	3.2	59.1	15.2
4	July 8-9, 1951	3.2	84.2	59.1	70.2
5	July 10-17, 1951	81.0	38.6	38.6	73.7
6	September 24-27, 1951	50.6	47.8	35.8	74.9
7	September 29-30, 1951	1.8	13.4	3.5	26.1
8	October 13-15, 1951	13.4	19.5	5.3	27.2
9	May 27-28, 1952	13.4	23.1	9.8	42.4
10	June 2, 1952	19.5	90.6	85.5	94.4
11	June 8-10, 1952	23.1	75.7	72.3	95.5
12	June 22-25, 1952	38.6	99.7	84.0	20.2
13	July 2-3, 1952	31.9	23.9	14.2	59.4
14	July 3-4, 1952	22.9	16.2	3.7	22.8
15	July 4, 1952	29.9	29.5	12.6	42.7
16	July 9-12, 1952	38.6	21.7	5.7	26.3
17	July 13-15, 1952	36.1	24.6	13.9	56.5
18	July 17-20, 1952	44.0	18.3	8.8	48.1
19	August 7-8, 1952	23.9	30.7	22.8	74.5
20	Aug. 31-Sep. 1, 1952	16.2	36.7	36.7	29.5
21	September 6-10, 1952	29.5	12.6	4.7	30.9
22	September 11-16, 1952	21.7	5.7	26.3	4.4
23	October 6-8, 1952	24.6	13.9	56.5	3.1
24	October 27-28, 1952	18.3	8.8	48.1	3.2
25	November 4-5, 1952	30.7	22.8	74.5	3.5
26	May 5-6, 1953	5.9	24.4	66.5	2.4
27	May 7-9, 1953	30.8	36.7	24.4	66.5
28	May 23-24, 1953	51.4	31.2	60.7	2.7
29	June 6-8, 1953	55.5	74.4	64.5	86.7
30	June 10-12, 1953	18.9	74.4	64.5	86.7
31	July 3-4, 1953	57.9	58.6	101.2	26.0
32	July 7-8, 1953	17.7	54.1	97.3	35.0
33	July 9-11, 1953	37.9	55.6	54.1	97.3
34	July 16-19, 1953	34.1	142.9	96.8	18.0
35	July 20, 1953	70.2	147.6	142.9	96.8
36	July 20-23, 1953	43.3	128.5	104.6	11.7
37	September 23-25, 1953	110.6	122.2	128.5	104.6
38	September 29-30, 1953	12.2	40.8	36.7	90.0
39	Sep. 30-Oct. 2, 1953	153	15.2	4.7	29.5
40	October 9, 1953	11.3	8.9	25.6	4.7
41	October 28, 1953	11.3	8.9	25.6	4.7
42	October 29-30, 1953	23.4	34.7	8.9	25.6

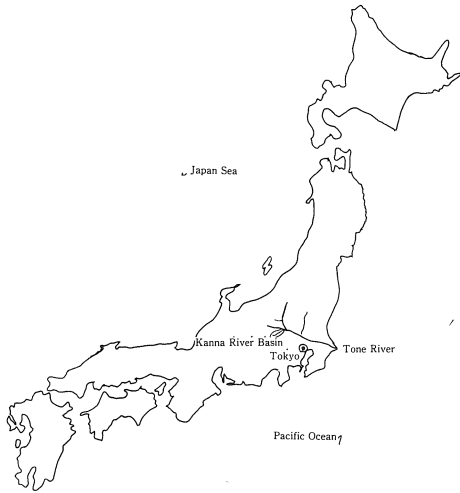


Fig. 1. Location of the experimental basin.

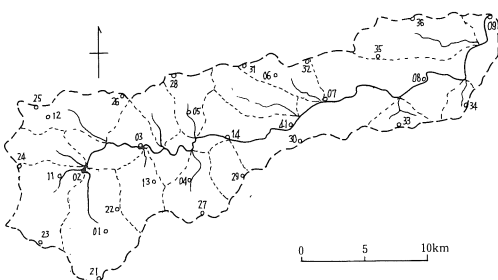


Fig. 2. Map of rain-gage network

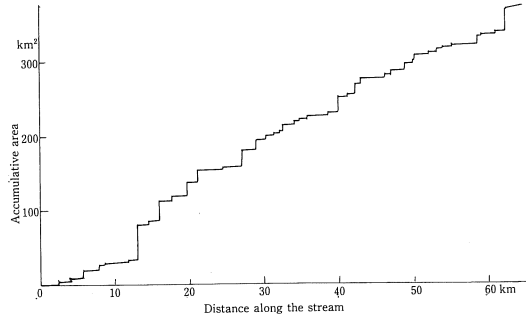


Fig. 3. Accumulative area

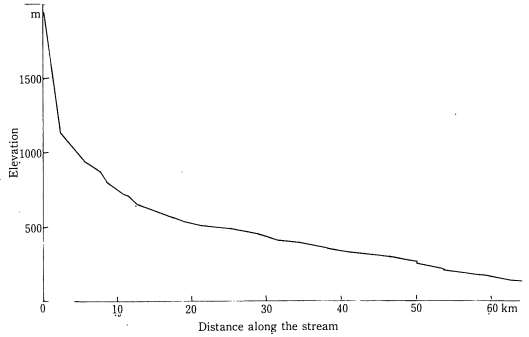


Fig. 4. Profile of the mainstream

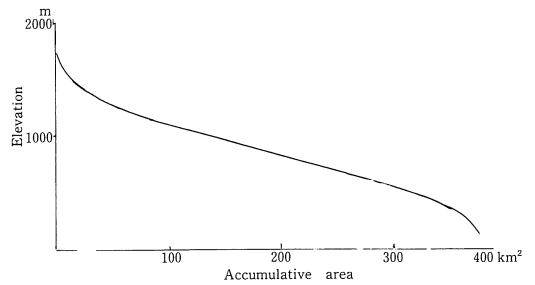


Fig. 5. Area-elevation curve

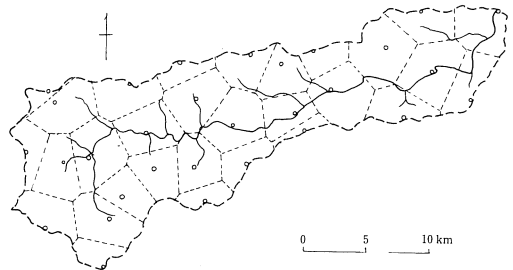


Fig. 6 (1) Thiessen polygon for 30 stations

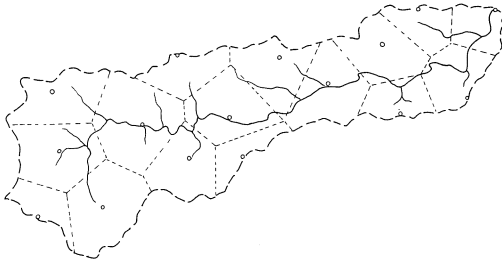


Fig. 6 (2) Thiessen polygon for 16 stations



Fig. 6 (3) Thiessenpolygon for 8 stations

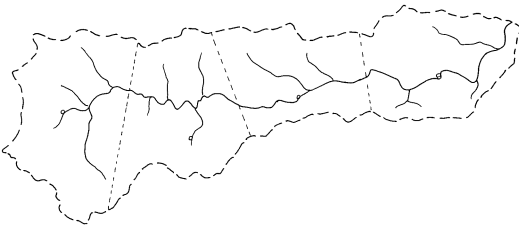


Fig. 6 (4) Thiessen polygon for 4 stations

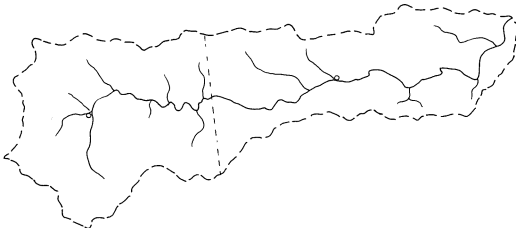


Fig. 6 (5) Thiessen polygon for 2 stations

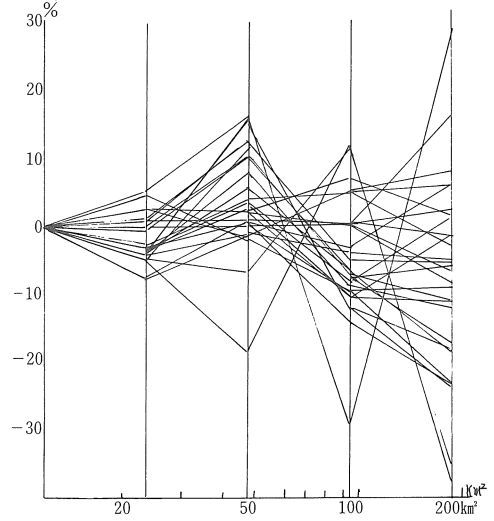


Fig. 7. Relation between the average governing area and the error in the Thiessen polygon method.

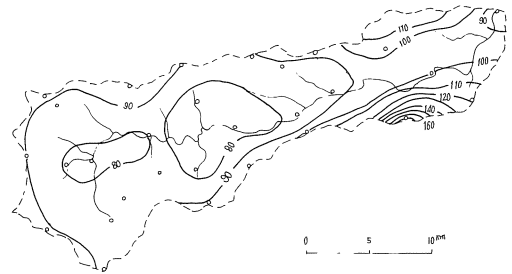


Fig. 8 (1) Isohyetal map for 30 stations in the case of No. 12 storm precipitation

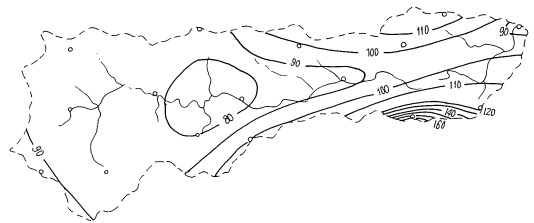


Fig. 8 (2) Isohyetal map for 16 stations in the case of No. 12 storm precipitation

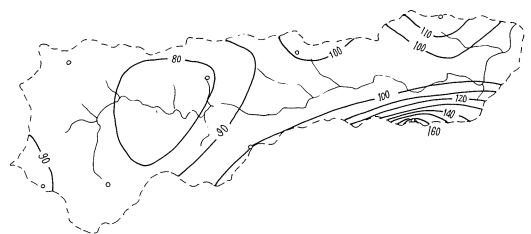


Fig. 8 (3) Isohyetal map for 8 stations in the case of No. 12 storm precipitation

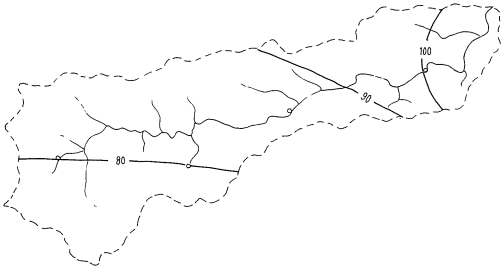


Fig. 8 (4) Isohyetal map for 4 stations in the case of No. 12 storm precipitation

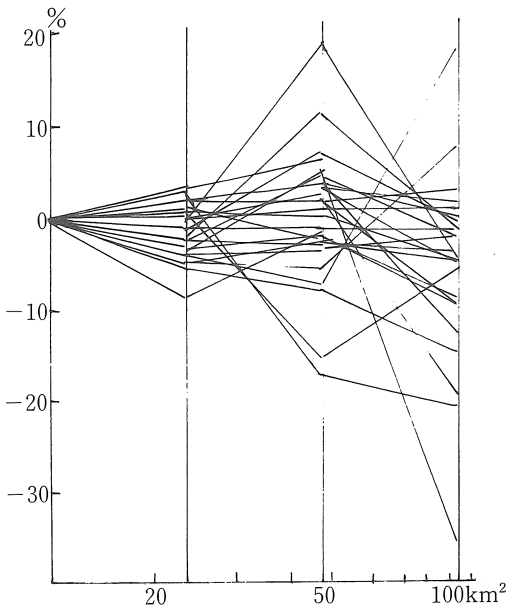


Fig. 9 Relation between the average governing area and the error in the isohyetal method

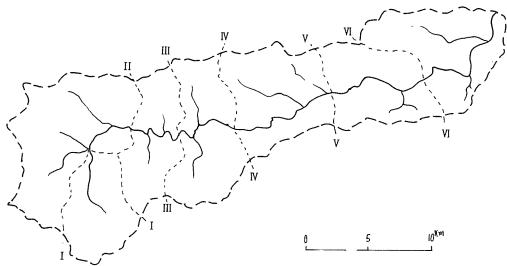


Fig. 10 Subdivision in the Original basin

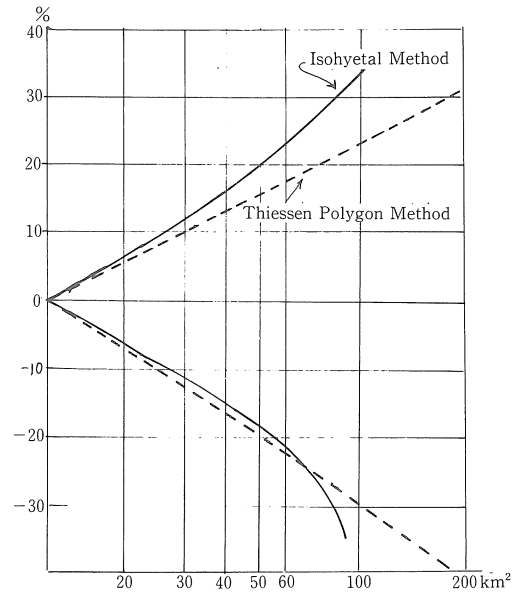


Fig. 11 Relation between the average governing area and the error for the envelopes of points in Fig. 7 and 8.

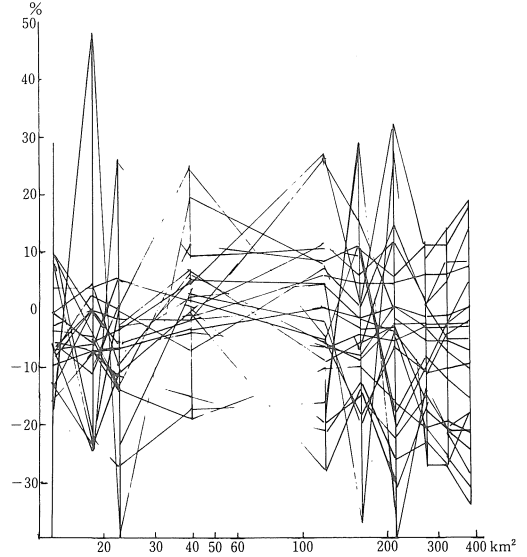


Fig. 12 Relation between the average governing area and the error in point rainfall method

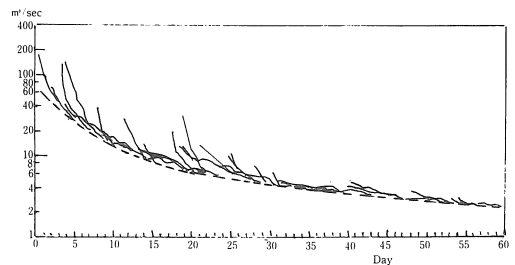


Fig. 13 Normal recession curve

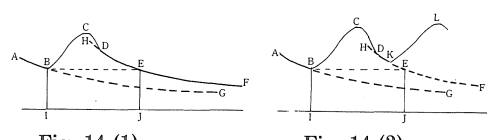


Fig. 14 (1)
Computation of runoff

Fig. 14 (2)
Computation of runoff

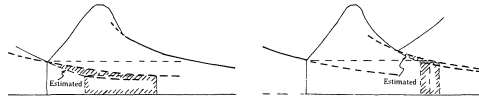


Fig. 14 (3)
Computation of runoff

Fig. 14 (4)
Computation of runoff

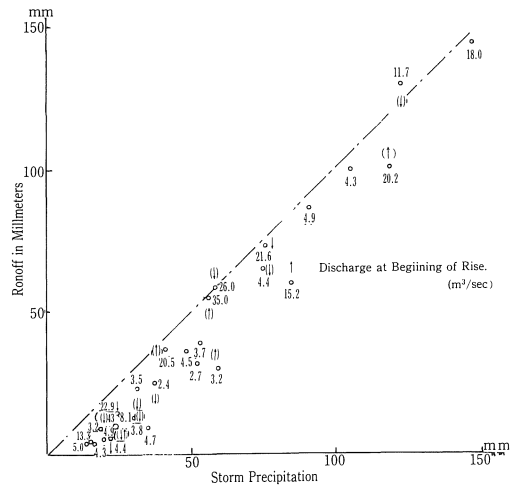


Fig. 15 Relation between storm precipitation discharge at beginning of rise and runoff

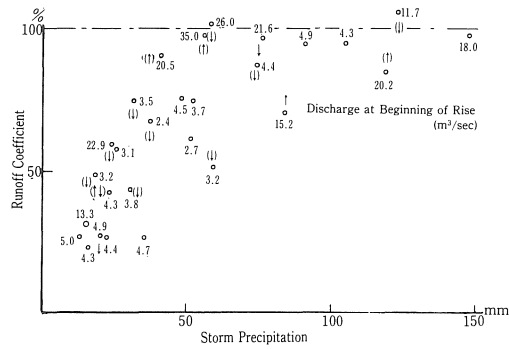


Fig. 16 Relation between storm precipitation, discharge at beginning of rise of rise and runoff coefficient